

## Flame Bands: CO + O chemiluminescence as a measure of gas temperature

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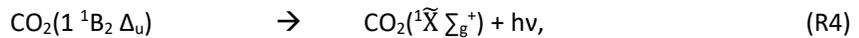
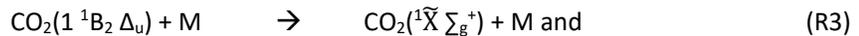
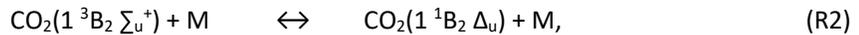
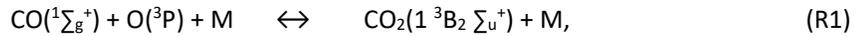
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### Abstract

Carbon monoxide flame band emission ( $\text{CO} + \text{O} \rightarrow \text{CO}_2 + h\nu$ ) in  $\text{CO}_2$  microwave plasma is quantified by obtaining absolute emission spectra at various locations in the plasma afterglow while simultaneously measuring gas temperatures using rotational Raman scattering. Comparison of our results to literature reveals a contribution of  $\text{O}_2$  Schumann-Runge UV emission at  $T > 1500$  K. This UV component likely results from the collisional exchange of energy between  $\text{CO}_2(^1\text{B})$  and  $\text{O}_2$ . Limiting further analysis to  $T < 1500$  K, we demonstrate the utility of CO flame band emission by analyzing afterglows at different plasma conditions. We show that the highest energy efficiency for CO production coincides with an operating condition where very little heat has been lost to the environment prior to  $\sim 3$  cm downstream, while simultaneously,  $T$  ends up below the level required to effectively freeze in CO. This observation demonstrates that, in  $\text{CO}_2$  plasma conversion, optimizing for energy efficiency does not require a sophisticated downstream cooling method.

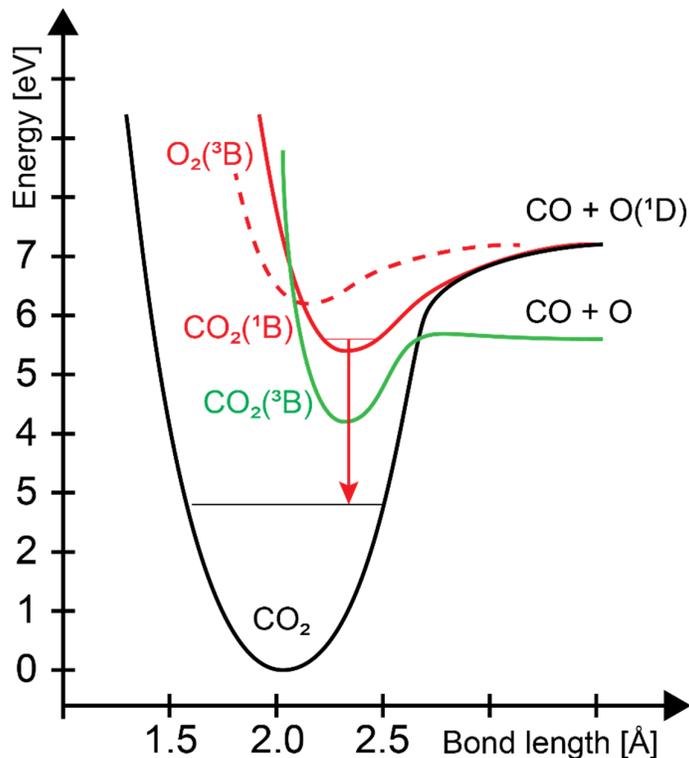
### 1. Introduction

Carbon monoxide flame bands are the result of recombination of CO and O to a highly excited electronic state of  $\text{CO}_2$  and consist of broadband emission of visible radiation, with extension into the UV. With ground state  $\text{CO}(^1\Sigma_g^+)$  and ground state  $\text{O}(^3\text{P})$  having different spin quantum numbers, a direct recombination to ground state  $\text{CO}_2(^1\tilde{\text{X}}\Sigma_g^+)$  cannot occur [1,2]. The recombination process must instead result from a chain of reactions such as:



where the initial recombination R1 leads to excited  $\text{CO}_2$  in a triplet state, which can undergo a (collision-induced) crossing over to excited  $\text{CO}_2$  in a singlet state via R2, which in turn can either be quenched to the ground state or undergo a radiative transition to the ground state of  $\text{CO}_2$  via R3 or R4, respectively [2–4]. It is the latter reaction which produces CO flame band emission. From this point onwards, the triplet state will be referred to as  $\text{CO}_2(^3\text{B})$ , the singlet as  $\text{CO}_2(^1\text{B})$  and the ground states of all species simply as CO, O and  $\text{CO}_2$ . It is important to note here that first principles calculations have revealed a significant overlap in the lowest electronically excited states of  $\text{CO}_2$ , so that  $\text{CO}_2(^3\text{B})$  and  $\text{CO}_2(^1\text{B})$  could be substituted by  $\text{CO}_2(^3\text{A})$  and  $\text{CO}_2(^1\text{A})$  [5,6]. The general scheme of R1 - R4 is assumed to be applicable

in either case since energy levels and dissociation limits for both singlets and triplets are *approximately* equal [2]. A schematic potential energy diagram along the OC-O bond length for  $\text{CO}_2$ ,  $\text{CO}_2(^3\text{B})$  and  $\text{CO}_2(^1\text{B})$  is depicted in Figure 1, which also includes the relative potential energy curve for the  $\text{O}_2(^3\text{B})$  state. The  $\text{O}_2(^3\text{B})$  state leads to  $\text{O}_2$  Schumann-Runge emission between 180 – 450 nm and has been observed in conjunction with CO flame band emission in  $\text{CO}_2$  mixtures [4].



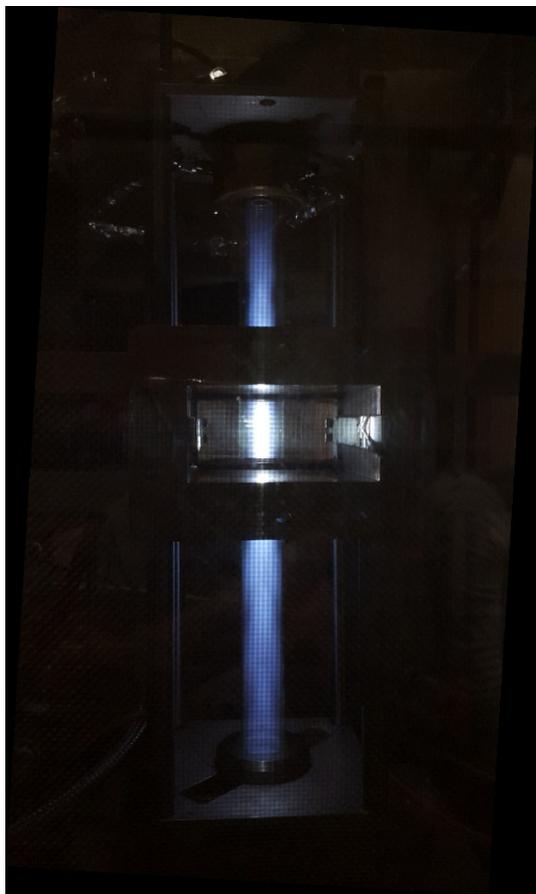
**Figure 1:** Schematic potential energy diagram along the OC-O bond length for  $\text{CO}_2$ ,  $\text{CO}_2(^3\text{B})$  and  $\text{CO}_2(^1\text{B})$ . The dashed line indicates the potential energy in  $\text{O}_2(^3\text{B})$  leading to  $\text{O}_2$  Schumann-Runge emission bands between 180 – 450 nm, which is included here for comparison without the O-O bond length being to scale [7].  $\text{CO}_2$  and  $\text{CO}_2(^1\text{B})$  dissociate into  $\text{CO} + \text{O}(^1\text{D})$  while  $\text{CO}_2(^3\text{B})$  dissociates into  $\text{CO}$  and  $\text{O}$ . The crossing over between  $\text{CO}_2(^3\text{B})$  and  $\text{CO}_2(^1\text{B})$  via R2 occurs where the green solid line and the red solid line overlap. The red arrow indicates a radiative transition from  $\text{CO}_2(^1\text{B})$  to  $\text{CO}_2$ .

Carbon monoxide flame band emission in a  $\text{CO}/\text{O}_2$  flame was first studied spectrographically by Burch in 1885 and 1886 [8,9], who reported a broadband emission spectrum across the visible range with different maxima in the green and violet. A more detailed investigation was performed by Weston in 1925 in  $\text{CO}/\text{O}_2$  and  $\text{CO}/\text{H}_2/\text{O}_2$  flames [10,11], from which it was concluded that the spectrum consists of a continuous background, with distinct, superimposed emission bands. Gaydon [12] and Clyne & Thrush [12,13] were the first to confirm the origins of CO flame bands via the recombination reaction R1. Dixon assigned its component bands to transitions between  $\text{CO}_2(^1\text{B}, v_1 = v_2 = v_3 = 0, 1) \rightarrow \text{CO}_2(2v_1 + v_2 = 20 - 30, v_3 = 0, 1)$  for wavelengths between 310 nm – 380 nm [14]. Because the upper electronic state  $\text{CO}_2(^1\text{B})$  is a strongly bent molecule, transitions to the linear ground state predominantly populate  $2v_1 + v_2$ , instead of the asymmetric stretching mode  $v_3$ . The reactions R1 – R4, then, predominantly produce ground state  $\text{CO}_2$  with highly excited combinations of the symmetric stretching mode  $v_1$  and bending mode  $v_2$  [15]. Since each of the many possible transitions brings with it a P- and R-branch, the resulting rovibrational spectrum is very dense in overlapping spectral features, creating a quasi-

continuous spectrum if observed with spectral resolutions less than 0.005 nm, explaining the continuum features observed by Burch and Weston. The aforementioned experiments in CO-containing flames at temperatures  $\leq 2200$  K were eventually supplemented by experiments in shock tubes, with which the temperature range for observing CO flame band emission was extended towards 3000 K [4,16,17].

The goal of this work is to map CO flame band spectra not in CO-containing flames, but in CO<sub>2</sub> plasma afterglows at various temperatures, with the purpose of using the spectral shape of the quasi-continuum as a measure of gas temperature. The absolute photon emission together with gas temperature can also serve as a measure for the CO + O recombination rate, or be used to obtain quantitative data on CO and O densities. Measuring absolute CO flame band emission at two or three specific wavelengths can allow for a fast 2D mapping of both gas temperature and the rate of back reactions occurring in the near-plasma and downstream portions of CO<sub>2</sub> plasma devices. This can be a valuable diagnostic for evaluating reactor performance or plasma model validation.

Two similar vortex-stabilized CO<sub>2</sub> microwave plasma reactors are used in this work. One is equipped for laser Raman scattering to obtain gas temperatures independently [18,19], and another is equipped for measuring CO flame band spectra over a large part of the afterglow using stepper motors. These reactors possess very high local plasma power densities of  $> 1$  GW/m<sup>3</sup> and large radial temperature gradients on the order of 2500 K/cm [20,21]. Due to the high plasma gas temperatures of  $> 3500$  K almost complete dissociation of CO<sub>2</sub> to CO + O occurs within the plasma region [19,21], which results in a luminous afterglow in the region surrounding the plasma. See Figure 2 for a photograph of the second plasma reactor used for large-scale afterglow mapping. With a high local CO and O density and a broad range of gas temperatures, these plasma reactors are well suited for studying CO flame band emission as a diagnostic tool in a pure CO<sub>2</sub> plasma environment .



**Figure 2:** Photograph of the vortex-stabilized microwave plasma reactor used for complete mapping of afterglows (operated here with a  $\text{CO}_2$  flow of 10 slm, pressure of 100 mbar and a microwave power of 1 kW). The plasma in the center of the waveguide is white, while blue afterglows extend above and below the waveguide, within the vortex flow structure created by tangential injection of  $\text{CO}_2$  at the top.

## 2. Theory & Approach

It has been empirically observed that reaction chains such as R1 - R4 can be expressed as a second order reaction [4,22,23], producing a wavelength-integrated emission intensity

$$I_\gamma = k_\gamma(T)[\text{CO}][\text{O}], \quad (1)$$

in units of  $\text{photons} \cdot \text{m}^{-3} \cdot \text{s}^{-1}$ , with  $[\text{CO}]$  and  $[\text{O}]$  the carbon monoxide and atomic oxygen number densities in  $\text{m}^{-3}$  and  $k_\gamma$  the rate coefficient in units of  $\text{photons} \cdot \text{m}^3 \cdot \text{s}^{-1}$ . Throughout this work  $k_\gamma(T) = 1.14 \cdot 10^{-24} e^{\frac{2080}{T}}$   $\text{photons} \cdot \text{m}^{-3} \cdot \text{s}^{-1}$  is assumed, based on measurements obtained by Slack & Grillo [23] and Myers & Bartle [4] for a temperature range of 1300 – 3000 K in a wavelength range of 260 – 800 nm. Note also that all results will be presented assuming a  $4\pi$  solid angle, so that steradians are not included in the units.

The details of how the rate coefficient  $k_\gamma$  relates to proposed reaction chains such as R1 - R4 has been an object of study for many decades, motivated by *e.g.* the use of the emission intensity  $I_\gamma$  as a means to determine the overall rate coefficient  $k_{rec}$  for the  $\text{CO} + \text{O}$  recombination reaction [24,25]:



A complete analysis of the various competing reaction chains in the literature is beyond the scope of this work, but an analysis for the reactions R1 - R4 is presented in the Supplementary Information. Here it suffices to mention a few general features:

- For most combinations of pressure and temperature, the quenching rate via R3 outstrips the spontaneous emission rate via R4, producing a simple relation between the (3<sup>rd</sup> order) overall recombination rate coefficient and the (2<sup>nd</sup> order) photon emission rate coefficient:

$$\frac{k_{rec}}{k_\gamma} = \frac{k_3^+}{k_4^+} \quad (2)$$

in units of m<sup>3</sup>. With the spontaneous emission rate  $k_4^+$  independent of temperature, and the quenching rate coefficient  $k_3^+$  typically assumed only weakly dependent on temperature, Eq. (2) illustrates the direct correspondence between  $k_\gamma$  and  $k_{rec}$ . The value of this ratio is typically on the order of 10<sup>20</sup> m<sup>-3</sup> at T > 1000 K [4,23,26,27].

- The identity of the third particle in the reaction chain has a limited effect on the value of  $k_\gamma$ , with M = Ar, He, N<sub>2</sub>, O<sub>2</sub> being the most thoroughly tested [28–30]. Pravilov and Smirnova have shown that O<sub>2</sub> can reduce  $k_\gamma$  by 10% for [O<sub>2</sub>] > 2·10<sup>21</sup> m<sup>-3</sup> for total pressures < 20 mbar and T < 300 K [3]. Third particle efficiencies for the overall reaction R5 with rate coefficient  $k_{rec}$  are summarized in a review by Baulch *et al.* [31], revealing an order of efficiencies He/Ne < Ar < N<sub>2</sub> < CO < CO<sub>2</sub> < O<sub>2</sub> with at least an order of magnitude difference from lowest to highest. Since  $k_{rec}$  scales directly with  $k_3^+$ , the third particle identity can significantly affect the ratio in Eq. (2) but may still leave the rate coefficient  $k_\gamma$  largely unaffected (see the Supplementary Information).
- The reaction chain R1 – R4 involves multiple collisions with a third particle M before CO<sub>2</sub>(<sup>1</sup>B) is formed, and the expected natural radiative lifetime of the CO<sub>2</sub>(<sup>1</sup>B) state is on the order of 100 ns [3,29]. It can be assumed that CO<sub>2</sub>(<sup>1</sup>B) is fully thermalized prior to the emission of a photon, since at the conditions investigated here, neutral-neutral collision frequency is estimated to be at least 50 times greater than the radiative lifetime of CO<sub>2</sub>(<sup>1</sup>B).

The main objective of this work is not to utilize wavelength-integrated photon emission intensities, but to infer gas temperatures from measured CO flame band spectra. Here we run into shortcomings of the current literature: transition moments for CO<sub>2</sub>(<sup>1</sup>B,  $v_1, v_2, v_3 > 0$ ) → CO<sub>2</sub>(2 $v_1+v_2 > 20, v_3 > 0$ ) are unavailable. Many first principles computational studies have focused on the inverse problem of CO<sub>2</sub> photolysis, where ground state CO<sub>2</sub> in low vibrational states is excited by UV photons to the CO<sub>2</sub>(<sup>1</sup>A) or CO<sub>2</sub>(<sup>1</sup>B) states and from there undergoing dissociation via the CO<sub>2</sub>(<sup>3</sup>A) or CO<sub>2</sub>(<sup>3</sup>B) states. Unfortunately, no data is provided for the transitions of highly vibrationally excited CO<sub>2</sub> [5,32,33], thus precluding the ability to accurately simulate the spectra of CO<sub>2</sub>(<sup>1</sup>B) from first principles at a given T. An exception to this is the work of Malerich and Scanlon, who used an harmonic oscillator approximation to obtain Franck-Condon factors for the CO<sub>2</sub>(<sup>1</sup>B) → CO<sub>2</sub> transitions to simulate spectra up to 900 K [34]. Since the validity of such an approximation towards higher temperatures and more highly vibrationally excited CO<sub>2</sub>(<sup>1</sup>B) is questionable; we take an empirical approach where CO flame band spectra are obtained over a wide range of gas temperatures. To this end, spatially resolved afterglow spectra are obtained from inverse Abel transforms of line-of-sight spectra at the exact locations a gas temperature is measured via laser-based rotational Raman scattering.

It has been observed that over small wavelength intervals the rate coefficient for photon emission  $k_\gamma$  can be described by an Arrhenius form [23,35], thus a wavelength-dependent emission intensity can be defined as:

$$I_\gamma^\lambda = \kappa_\gamma^\lambda(T)[\text{CO}][\text{O}] \text{ and} \quad (3)$$

$$\kappa_\gamma^\lambda(T) = \kappa_0^\lambda e^{-\frac{E_a^\lambda}{T}}, \quad (4)$$

with units of photons.m<sup>-3</sup>s<sup>-1</sup>nm<sup>-1</sup> and photons.m<sup>3</sup>s<sup>-1</sup>nm<sup>-1</sup> respectively. The superscript  $\lambda$  indicates a discrete wavelength interval and  $\kappa_0^\lambda$  and  $E_a^\lambda$  a wavelength-dependent pre-factor and activation energy respectively.

Obtaining values for  $\kappa_0^\lambda$  and  $E_a^\lambda$  from measured spectra not only requires knowledge of  $T$ , but also of the [CO] and [O] densities. To circumvent this, we rely on the rate coefficient for the wavelength-integrated emission intensity

$$[\text{CO}][\text{O}] = \frac{I_\gamma}{\kappa_\gamma(T)}, \quad (5)$$

which simultaneously ensures that the wavelength-dependent components add up to the wavelength-dependent rate coefficient:

$$k_\gamma(T) = \sum_\lambda \kappa_0^\lambda e^{-\frac{E_a^\lambda}{T}} \Delta\lambda, \quad (6)$$

with  $\Delta\lambda$  as the wavelength interval. For both Eqs. (5) and (6) the wavelength range appropriate to the literature value of  $k_\gamma(T)$  is used. A full error propagation is included in the final results for  $\kappa_0^\lambda$  and  $E_a^\lambda$  presented below, including the relative errors in absolute calibration of the spectrometer from repeated wavelength-dependent calibrations, spectrometer signal noise, estimated errors in the inverse Abel transform applied to the as-measured line-of-sight spectra, and measurement errors in the [CO][O] values obtained via Eq. (5). For the latter, this includes the measurement error in  $I_\gamma$  and the measurement error in  $T$  obtained via rotational Raman scattering. The systematic error arising from our chosen values of  $k_\gamma$  is not included.

### 3. Experimental setup

The experimental setup consists of a microwave source, a vortex flow reactor, laser scattering diagnostics, and parabolic mirror optics, as shown schematically in Figure 3.

#### 3.1 Microwave plasma reactor

Microwaves are generated using a cavity magnetron source operated in continuous mode, producing radiation at 2.45 GHz. The magnetron has an adjustable power between 200 - 1400 W. The microwave radiation is coupled to a rectangular WR-340 waveguide via a three stub tuner. Manual tuning of the stubs ensures near-perfect matching to the plasma load, with reflected power losses < 3%.

A quartz tube (30 mm outer diameter, 27 mm inner diameter, and 400 mm length), acting as a microwave-transparent flow reactor, is inserted perpendicularly through the waveguide. The waveguide is short-circuited with a movable plunger at a quarter wavelength distance from the center of the tube, such that a standing wave is sustained in the cavity with the maximum electric field at the center of the quartz tube. A CO<sub>2</sub> gas flow between 6 – 12 slm is injected into the quartz tube via two 3 mm inner diameter nozzles. These nozzles are fitted tangentially and off-centered to the tube axis so that the resulting flow inside the quartz tube consists of an outer vortex spiraling to the downstream

region, with the inner regions of the tube subjected to an induced secondary vortex. This plasma-sustaining region is dominated by an upward flow, circulating back towards the injection nozzles [21,36]. The quartz tube, and surrounding vacuum components, are pumped using dry pumps in combination with a needle valve, allowing for an operating pressure between 7 mbar (ignition pressure of the plasma) and 1000 mbar. A more detailed treatment of the microwave reactor can be found in [37].

### **3.2 Raman scattering**

A frequency-doubled laser ( $\lambda = 532$  nm, Spectra-Physics GCR 230) operated at 5 W and 10 Hz is used for the laser Raman scattering, see Figure 3(a). The beam is first enlarged by a factor 4 using a telescope (not shown in Figure 3) and is then focused 4 cm upstream of the center of the plasma with an  $f = 2$  m lens, where afterglow emission is dominant. Enlargement of the laser beam using the telescope ensures that the beam focusing at the measurement point can be approximated well with linear optics. Light scattered by the gas is collected perpendicularly to the laser beam with an achromatic doublet with  $f = 100$  mm. A 1:1 image is projected onto a fiber bundle ( $27 \times 400$   $\mu\text{m}$ ) that is used to illuminate a custom-built Littrow spectrometer ( $f = 1$  m, lens diameter  $d = 100$  mm,  $f\# = f/d = 10$ , dispersion of 0:85 nm/mm), equipped with an iCCD (Princeton Instruments PiMax 4). A long-pass filter with a cutoff wavelength of 550 nm (ThorLabs FGL550) is placed in front of the collection fibers to block scattered light at the laser wavelength from entering the spectrometer. In other words, only light that loses energy upon scattering is measured (*i.e.* the Stokes branch).

The reactor is mounted on a linear stage, which allows for lateral translation with respect to the probe laser beam, making radial scans possible. Rotational Raman spectra are measured with  $< 1$  mm radial resolution, determined by the beam waist. More details regarding this setup can be found in [38].

Integration times on the order of 30 minutes, in combination with maximum intensification, are used to produce spectra that are fitted for each fiber individually, with only rotational temperature ( $T_{rot}$ ) as a fitting parameter. Details for the spectrum fitting approach can be found in [15]. Rotational temperature as a function of fiber number (*i.e.*, axial position in the quartz tube) can be fitted well to an exponential decay function, providing a check on outliers in the data and reducing the measurement error for  $T$  to 5% – 10% in most cases.

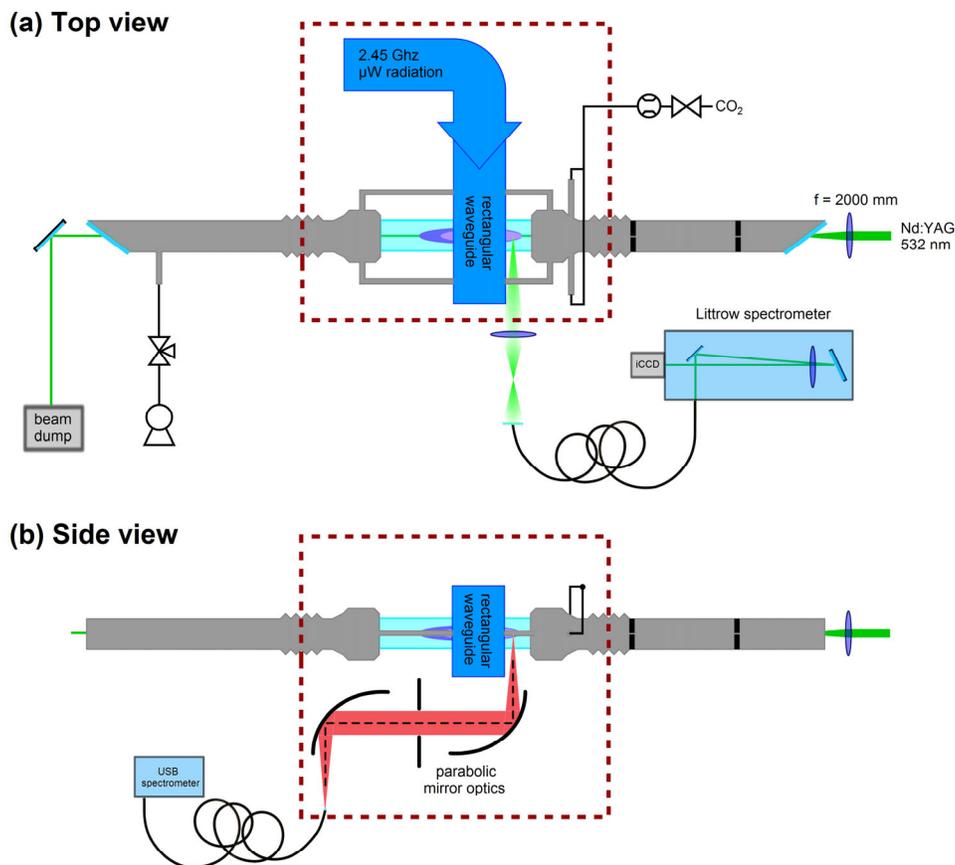
### **3.3 Flame band mirror optics**

Afterglow emission was measured via two parabolic mirrors (Thorlabs MPD129-F01) in combination with a USB spectrometer (Thorlabs Flame-S), see Figure 3(b). The first mirror has its  $90^\circ$  off-axis focus ( $f = 2''$ ) placed at the same location as the Raman laser scattering setup. The resulting parallel beam is focused onto an optical fiber using a second, identical mirror. In the path of the parallel beam between the mirrors, an iris is placed with an opening of 6.9 mm, so that the solid angle for light collection is set at  $\Omega = 1.45 \cdot 10^{-2}$  sr. With this low solid angle, measurements are effectively line-of-sight along a 200  $\mu\text{m}$  diameter cylindrical region through the quartz tube. If measurements are performed as a function of radial position in the quartz tube, discrete inverse Abel transforms are performed using the formalism described in [39].

Using parabolic mirrors instead of lenses ensures no chromatic aberration occurs over the broad wavelength range being measured. Moreover, UV enhanced aluminum was used as a mirror coating, providing 85 - 95% reflectance between 240 - 700 nm. The spectrometer utilizes a 600 lines/mm grating blazed at 300 nm, providing an efficiency between 30 – 70% over the wavelength range of interest. A 20 cm, 200  $\mu\text{m}$ , multimode UV fiber is used to minimize losses in the UV between mirror optics and spectrometer. The spectrometer was fitted with a 200  $\mu\text{m}$  entrance slit, so that all light from

the fiber is coupled into the spectrometer, at the expense of a low spectral resolution of 8 nm. In order to enhance signal-to-noise further, spectra are binned over 10 nm intervals (combining the output of 22 pixels).

Absolute calibration of the quartz tube wall + mirror optics + spectrometer using D<sub>2</sub> (240 – 400 nm) and halogen lamps (400 – 700 nm) found a minimum sensitivity of  $2.4 \cdot 10^{-8}$   $\mu\text{J}/\text{count}$  (or  $2.9 \cdot 10^4$  photons/count) at  $240 \pm 5$  nm and a maximum sensitivity of  $1.2 \cdot 10^{-9}$   $\mu\text{J}/\text{count}$  (or  $3.0 \cdot 10^3$  photons/count) at  $500 \pm 5$  nm. All spectra presented in this work, including normalized spectra in arbitrary units, are based on calibrated intensities in units of photons/nm/m<sup>2</sup> (line-of-sight spectra) or photons/nm/m<sup>3</sup> (Abel-inverted spectra).



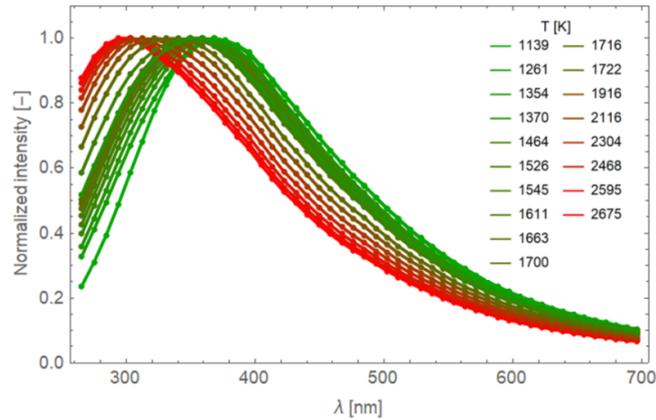
**Figure 3:** Schematic (a) top and (b) side views of the microwave plasma reactor used for obtaining CO flame band spectra and independent temperature measurements via rotational Raman scattering. In this reactor, the laser + Raman collection optics and the CO flame band optics are focused on the same location in the afterglow region, which remains fixed. To obtain data in the radial direction, the waveguide + quartz tube assembly is moved up or down along the page in the top view.

## 4. Results & Discussion

### 4.1 Constructing an empirical model for CO flame bands

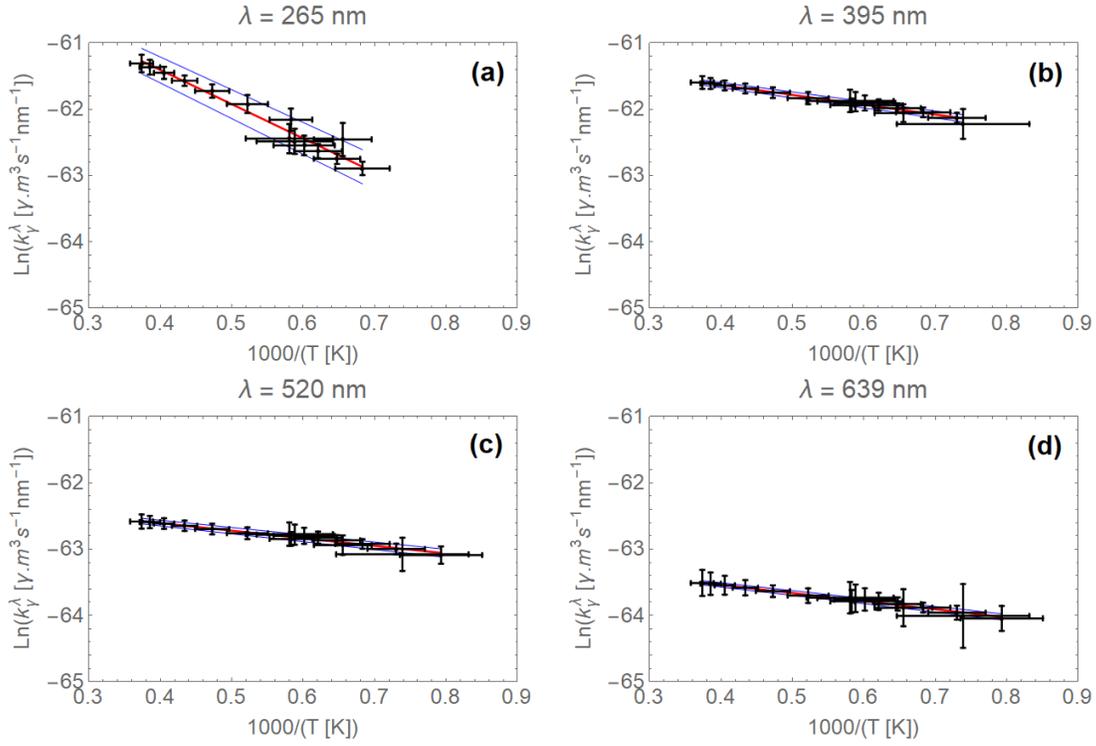
Two radial scans of (line-of-sight integrated) CO flame band spectra and (local) rotational Raman spectra were collected 4 cm from the center of the plasma (2 cm into the afterglow above the waveguide) at input powers of 330 W and 1000 W, pressures 200 mbar and 260 mbar, and input flow

rates of CO<sub>2</sub> of 7 slm and 8 slm. The CO flame band spectra were subsequently Abel-inverted to obtain local spectra. The resulting CO flame band spectra are shown in Figure 4, where they are normalized to their maximum intensity values to allow for an easy comparison of the spectrum shape. As can be seen in Figure 4, there is a clear shift of the intensity maximum with increasing temperature, an effect previously observed by Slack & Grillo in spectra obtained at 1300 K and 2700 K [23].



**Figure 4:** Abel-inverted afterglow spectra normalized at their maximum intensity values. Gas temperatures  $T$  indicated in the legend are obtained from rotational Raman scattering. A clear shift towards shorter wavelengths is observed with increasing gas temperature.

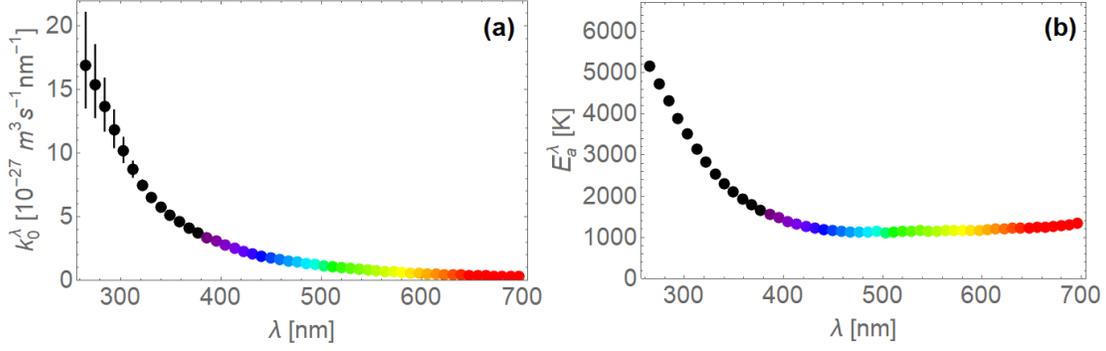
With the gas temperatures known through the use of rotational Raman scattering, Eq. (5) was used to obtain the product  $[CO][O]$  for all conditions, so that the intensity data  $I_{\gamma}^{\lambda}$  could be corrected to rate coefficients  $\kappa_{\gamma}^{\lambda}$  in units of photons.m<sup>3</sup>s<sup>-1</sup>nm<sup>-1</sup> at every wavelength. All available data was then used to create Arrhenius plots at wavelengths between 265 nm and 700 nm, in steps of approximately 10 nm. Examples of these Arrhenius plots, including fits to Eq. (4), are depicted in Figure 5. As seen in this figure,  $\kappa_{\gamma}^{\lambda}$  follows the Arrhenius-type behavior within the measurement error at all wavelengths. The only substantial deviations occur at wavelengths below 300 nm, with a typical example at  $\lambda = 265$  nm shown in Figure 5(a).



**Figure 5:** Wavelength- dependent Arrhenius fits at four selected wavelength intervals. For the measured data, error bars in the vertical direction include (relative) errors in absolute calibration of the spectrometer, spectrometer signal noise, estimated errors in the Abel inversion and errors in the  $[CO][O]$  values used to calibrate the data. Error bars in the horizontal direction indicate the error in the rotational Raman temperature measurements. The central straight line (red) is the least-squared fit, with the blue straight lines indicating the extrema of the fit based on the  $1\text{-}\sigma$  error of the two fitted parameters  $\kappa_0^\lambda$  and  $E_a^\lambda$ .

The sizable horizontal error bars at lower  $T$  in Figure 5 are a consequence of scatter in repeated rotational Raman spectra at a given position and measurement condition. While Raman spectra can be obtained with higher signal-to-noise at lower  $T$  (and thus, higher neutral gas density), the lower  $T$  points are found near the edge of the quartz tube. Near the tube edge, however, vortex flow instabilities can lead to shifts in temperature during accumulation of spectra. In the UV, such as in Figure 5(a), the lower  $T$  points are missing as a direct consequence of the  $CO_2(^1B)$  emission being well below the detection limit of the optical system at these wavelengths.

Results for Arrhenius pre-factors  $\kappa_0^\lambda$  and activation energies  $E_a^\lambda$  from the error-weighted linear regressions in Figure 5 are shown in Figure 6(a,b). Here it becomes evident that both  $\kappa_0^\lambda$  and  $E_a^\lambda$  increase towards the UV, with  $E_a^\lambda$  mostly leveling off for  $\lambda > 450$  nm. Note that while values for  $\kappa_0^\lambda$  depend on the choice of  $k_\gamma(T)$ , activation energies  $E_a^\lambda$  are absolute and depend directly on the measured rotational Raman temperatures.



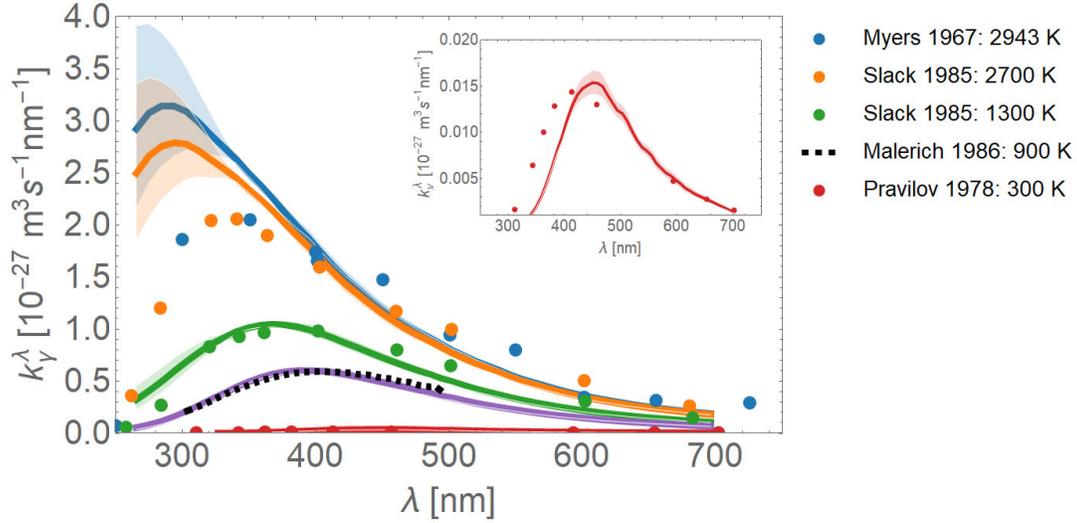
**Figure 6:** Wavelength-dependent Arrhenius coefficients  $k_0^\lambda$  and  $E_a^\lambda$ . Error bars are indicated, but for  $E_a^\lambda$  fall within the point size. Colors indicate the visible spectrum. All data points are tabulated in the Supplementary Information.

At  $\lambda > 400$  nm,  $E_a^\lambda$  is relatively constant at 1100 K (or 0.09 eV), less than the wavelength-averaged activation energy of 2080 K (or 0.18 eV) assumed for  $k_\gamma$ . From the relation between the overall recombination rate coefficient  $k_{rec}$  and  $k_\gamma$  in Eq. (2), the only difference in activation energies between these two rate coefficients comes from the activation energy for quenching of the  $\text{CO}_2(^1\text{B})$  state via R3, which itself might depend on wavelength (or, more accurately, the internal state of  $\text{CO}_2(^1\text{B})$ ). Figure 5 perfectly illustrates why determinations of  $k_{rec}$  from CO flame bands lead to lower activation energies for R5 at low  $T$  (where only emission  $> 300$  nm can be distinguished) than in similar experiments performed at higher  $T$ , see *e.g.* [23,30]. Rate coefficients for  $k_{rec}$  from more absolute measurement techniques are preferred, with comparison to  $k_\gamma$  at best providing some insight into the quenching behavior: taking the commonly used activation energy of 1510 K for  $k_{rec}$  from Tsang & Hampson [26], we can conclude that quenching of  $\text{CO}_2(^1\text{B})$  at  $\lambda > 400$  nm has an activation energy of  $\sim 400$  K.

The pre-factor  $k_0^\lambda$  fits very well to a power law:

$$k_0^\lambda \approx 2.78 \cdot 10^{-16} \cdot \lambda^{-4.21}. \quad (7)$$

Part of this rapid increase of pre-factor at shorter wavelengths may be accounted for by a decrease in the natural radiative lifetime in R4 at higher energies. Since the time between molecular collisions at the conditions used here is approximately 2 ns, and the natural radiative lifetime of the  $\text{CO}_2(^1\text{B})$  state is at least 200 ns [3,30], full thermalization of this state is expected to occur prior to reaction R4. With the final state of  $\text{CO}_2(^1\text{B})$  from which photon emission occurs not depending strongly on its history via reactions R1 and R2, the most likely candidate for affecting  $k_0^\lambda$  is the quenching reaction R3. A strong reduction in the probability for R3 with  $\text{CO}_2(^1\text{B}, v_1=v_2=v_3>0)$  would translate to a substantial increase in  $k_0^\lambda$  at shorter wavelengths.



**Figure 7:** Wavelength-dependent rate coefficients  $\kappa_Y^\lambda$  derived in this work (solid lines) compared to literature sources (points, with the dashed line for Malerich indicating a simulated spectrum) [3,4,23,34]. The inset shows a zoom on the Pravilov comparison at 300 K. Note that Myers, Malerich and Pravilov data extend beyond the temperature range investigated in this work by + 300 K, - 200 K and - 840 K respectively, so that the solid lines represent extrapolations.

#### 4.2 Comparison of the empirical model to literature

An alternative interpretation for results of  $\kappa_0^\lambda$  and  $E_a^\lambda$  at  $\lambda < 400$  nm becomes necessary after comparison to previously measured  $\kappa_Y^\lambda$  data in Figure 7. The correspondence at  $\lambda > 400$  nm is very reasonable, and the approximate spectral simulation by Malerich & Scanlon matches very well with the empirical model employed here, despite the latter being extrapolated by 200 K below the minimum measured temperature [34]. The extrapolation is still accurate when extended down to 300 K, as shown in the inset of Figure 7. It is worth noting that if our empirical model is produced based on data obtained only at 200 mbar (and neglecting the higher temperature data obtained at 260 mbar), the correspondence with the 300 K data obtained by Pravilov & Smirnova is further improved [3]. This serves to indicate that our empirical model for  $\kappa_Y^\lambda$  could be further refined with the inclusion of lower temperatures. The most significant deviation between the current work and literature data occurs in the UV region at higher  $T$ : our data predicts a much higher UV component. The most significant differences between the current work and that of Myers & Bartle [4] and Slack & Grillo [23] are:

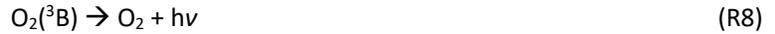
- (i) our proximity to an active plasma, a potential source of additional excited species,
- (ii) their use of shock tubes operated at peak pressures of 1.5 – 3.0 bar to obtain high peak temperatures and subsequent dissociation of  $O_2$  or  $O_3$  to atomic O, and
- (iii) their typical gas composition of  $CO_2:CO:O:O_2:Ar \approx 10:10:1:1:78$ , while at the highest temperatures measured here the estimated composition of the afterglow is  $CO_2:CO:O:O_2:Ar \approx 60:25:5:10:0$  [21].

Regarding (i), the estimated time-of-flight to the measurement location 2 cm away from the plasma is 1 – 2 ms, so that at best metastable excited species will survive. However, with predominantly CO and O emerging from the plasma, no obvious candidate metastable species leading to emission further

downstream present themselves. Similarly, ion densities are likely far too low to lead to significant rates of radiative ion-electron recombination reactions. This conclusion is supported by the fact that at lower  $T$  the afterglow spectra from plasma are almost equal to spectra obtained in the thermal flame and shock tube conditions depicted in Figure 7.

For (ii), it may be reasonable to expect that the much higher pressures employed by Myers & Bartle and Slack & Grillo lead to proportionally more quenching of highly excited  $\text{CO}_2(^1\text{B}, v_1 = v_2 = v_3 > 0)$  so that the UV component is strongly reduced. As discussed previously, the time between collisions is already significantly shorter than the natural radiative lifetime of the excited state at our reduced pressures [3,30], therefore, we do not consider this a sufficient explanation.

Regarding (iii), both authors determine that  $\text{O}_2$  does not lead to significant *additional* quenching. However, an alternative mechanism is suggested by Myers & Bartle [4], as well as by Pravilov & Smirnova [30]:



where R8 leads to emission of  $\text{O}_2$  Schumann-Runge bands between 180 – 450 nm. Referring back to Figure 1, exchange of energy between  $\text{CO}_2(^1\text{B})$  and  $\text{O}_2$  is quite likely considering the overlap in potential energy between  $\text{CO}_2(^1\text{B})$  and  $\text{O}_2(^3\text{B})$ . Energy levels close to resonance might exist between these two states, allowing for reaction R6 to proceed at a sufficient rate. Comparing the difference between our result and the experiment of Myers & Bartle, we indeed find a good correspondence with the  $\text{O}_2$  Schumann-Runge bands, see Figure 8. When calculating the expected emission based on R1 – R8 we find (see the Supplementary Information for a derivation):

$$I_{\gamma}^{\text{O}_2} \approx \frac{k_6^+ k_8^+}{k_4^+ k_7^+} X_{\text{O}_2} \cdot I_{\gamma} \propto X_{\text{O}_2} \cdot [\text{CO}][\text{O}], \quad (8)$$

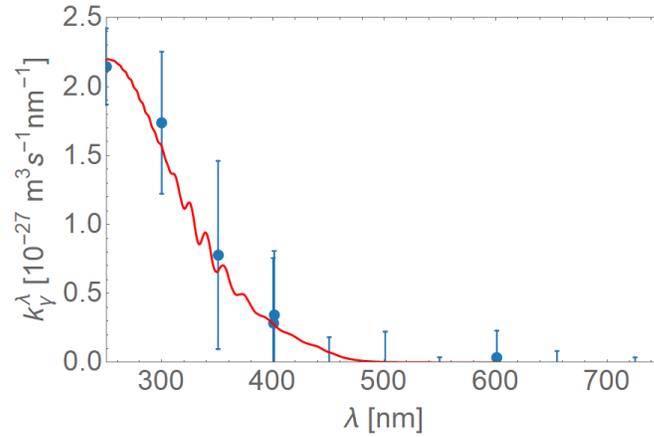
revealing that this mechanism is (a) proportional to the molecular oxygen fraction  $X_{\text{O}_2}$  and (b) proportional to CO + O flame band emission  $I_{\gamma}$ . Because our  $\text{O}_2$  concentration is expected to be significantly higher than in the shock tube experiments, the mechanism of R6 - R7 would produce far more  $\text{O}_2$  Schumann-Runge emission. Furthermore, since it would scale directly with  $[\text{CO}][\text{O}]$ , it is not easily distinguished in the Arrhenius plots of Figure 5, and does not lead to significant discontinuities in the values of  $\kappa_a^\lambda$  and  $E_a^\lambda$  as a function of wavelength. The small offsets observed at  $\lambda < 300$  nm, such as in Figure 5(a), may be caused by differences in  $X_{\text{O}_2}$  at the different measurement positions, however.

Another channel for the emergence of  $\text{O}_2$  Schumann-Runge emission occurs via the recombination of atomic oxygen in the electronic ground-state leading to the overall reaction:



This chemiluminescent process has been shown to have a high activation energy of  $\sim 14000$  K and can account for at most 20% of the observed UV radiation [4,40,41]. If this process were dominant in the production of  $\text{O}_2$  Schumann-Runge emission, it would reveal itself by a much greater increase in

$E_a^\lambda$  towards lower wavelengths in Figure 6 than is currently observed. Therefore, it can be concluded that reaction chain R6 - R8 is the probable origin of the excess UV emission.



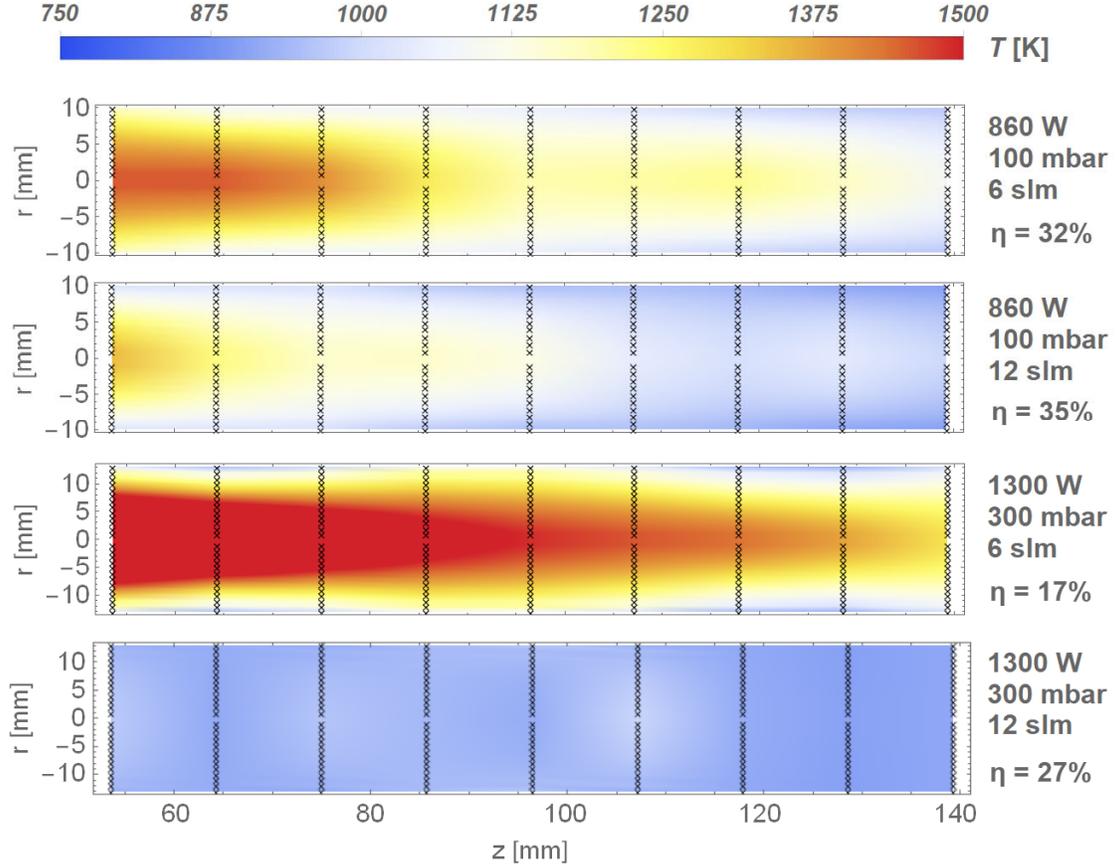
**Figure 8:** The difference between our model and the data of Myers & Bartle [4] (points) to a simulated  $O_2$  Schumann-Runge spectrum at  $T = T_{rot} = T_{vib} = 2943$  K (solid line). The error bars indicate only the measurement error from Myers & Bartle.

A definitive analysis of the UV emission at increased temperature will require a high resolution study of the spectrum to identify individual transitions. Combined with our recent development of obtaining a direct measurement of [CO], [O] and [ $O_2$ ] from rotational Raman data [19], the contributions of  $I_Y^{O_2}$  in Eq. (8) and  $I_Y$  in Eq. (3) to the total spectrum can be disentangled. Based on current data, we argue that our results are representative of CO flame band emission up to temperatures of at least 1500 K. At higher temperatures the unknown atomic and molecular oxygen fractions may lead to deviations of the Arrhenius model based on the coefficients in Figure 6.

#### 4.3 Application of the CO flame band Arrhenius model: elucidating post-plasma cooling

As a demonstration of our proposed method, we apply the Arrhenius model on the microwave plasma reactor depicted in Figure 2 at operating conditions close to the original measurements on which the empirical model is based. Line-of-sight spectra were obtained along the width of the tube every 1 mm and along the length of the tube every 1 cm. After applying the Abel inversion to the spectra obtained along the width of the tube (forcing symmetry in the radial direction), the Arrhenius model was fitted to the spectra, and a temperature obtained (see the Supplementary Information for example fits). Resulting temperature maps for locations downstream of the plasma are depicted in Figure 9, at plasma powers of 860 W and 1300 W, pressures of 100 mbar and 300 mbar and  $CO_2$  input flows of 6 and 12 slm. Residuals of the Arrhenius model fits to the measured spectra are  $< 5\%$  at all wavelengths and all positions for this data, including those for the 300 mbar, 6 slm data where the maximum fitted temperature is 1950 K. At this position there is already significant UV emission at  $\lambda = 260$  nm, indicative of the  $O_2$  Schumann-Runge emission discussed above. Considering that the quality of the fit is not adversely affected, we tentatively conclude that  $X_{O_2}$  depends only on  $T$  and not on *e.g.* pressure or time-of-flight of species from the plasma. The quality of the fit is adversely affected for spectra obtained closer to the plasma at 300 mbar, such as exactly to the side of the ( $\sim 3$  mm wide) plasma within the waveguide, where gas temperature may increase to  $> 3000$  K [20]. Results for these

positions are therefore not included here, with future work aiming to extend our understanding of afterglows in pure CO<sub>2</sub> plasma towards higher temperatures.



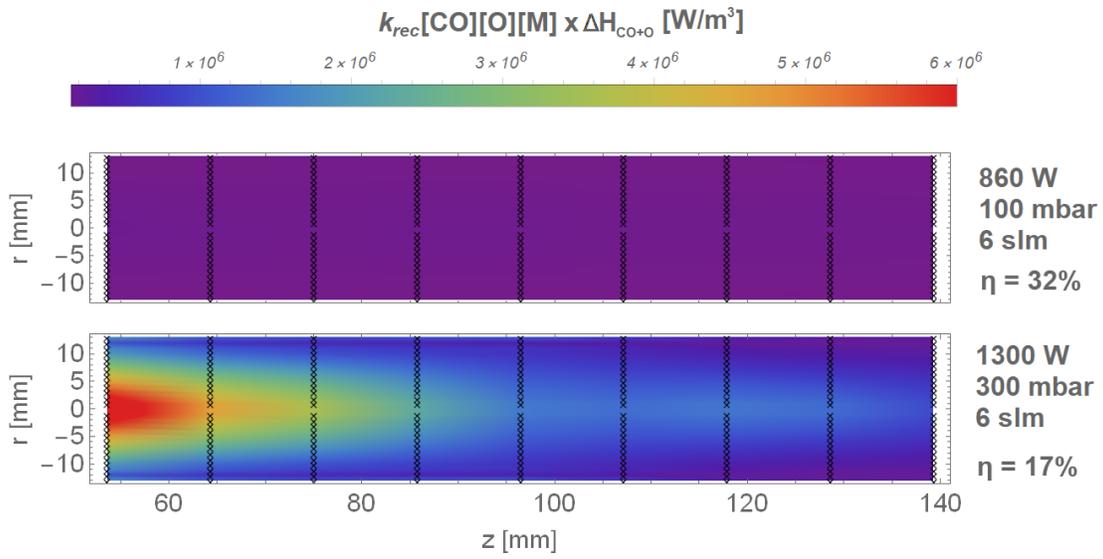
**Figure 9:** Example temperature maps in the afterglow. Maximum  $T$  for the 300 mbar, 6 slm data is 1950 K. Crosses indicate the original measurement positions. The coordinates on the horizontal axis increase in the downstream direction, with  $z = 0$  mm located at the center of the waveguide (coinciding with the approximate center of the plasma; the bottom edge of the plasma is located at  $z \approx 20$  mm). The residuals of the Arrhenius model fits to the measured spectra are  $< 5\%$  at all wavelengths and all positions for this data. Energy efficiency  $\eta$  for CO creation for each condition is also indicated.

#### 4.3.1 CO losses and heat generated in the downstream region

Analyzing the temperature maps of Figure 9 for the region at least 3 cm downstream of the plasma ( $z > 53$  mm), we observe that the decrease of  $T$  along the length of the tube depends strongly on flow and pressure. Both a reduction in pressure and an increase in flow rate imply a shorter time-of-flight from the bottom end of the plasma to the measured positions in Figure 9. The peak temperature in the plasma is  $\sim 3500$  K at 100 mbar and  $\sim 6000$  K at 300 mbar, irrespective of flow rate [20,21]. Nonetheless, we observe much lower temperatures in the downstream region at 12 slm versus 6 slm for both pressures. The effect of doubling the flow is also more significant for the 300 mbar data. The highest energy efficiencies  $\eta$  for the complete CO<sub>2</sub> conversion process, also indicated in Figure 9, coincide with temperatures already being below 1500 K at 3 cm below the plasma. Losses of CO within the afterglow region covered in Figure 9 can be evaluated as follows:

$$\rho_{CO+O} = k_{rec}(T)[CO][O][M] \cdot \Delta H_{CO+O}(T), \quad (9)$$

where  $\rho_{CO+O}$  is the heat production in  $W/m^3$  from CO + O recombination via R5,  $k_{rec} = 1.7 \cdot 10^{-45} e^{-\frac{1510}{T}}$   $m^6s^{-1}$  the rate coefficient for this reaction via Tsang & Hampson [26], the product  $[CO][O]$  in  $m^6$  as obtained from the integrated emission intensity  $I_\gamma$  via Eq. (3) and  $\Delta H_{CO+O}(T)$  the change in enthalpy for this reaction in  $J$ . The results of applying Eq. (9) to our data in Figure 9 are shown in Figure 10 for the two 6 slm conditions, which can be expected to have the most recombination. Integrating  $\rho_{CO+O}$  over the measured region (in cylindrical coordinates) provides the heat generated in the afterglow from CO + O reactions: 2.2 W at 100 mbar and 48 W at 300 mbar. Though certainly a negligible loss at 100 mbar, at 300 mbar this equates to a loss of  $\sim 10\%$  of CO molecules along the length of the tube within the measured region. Improved quenching in this region would therefore allow for a modest increase of  $\eta$  from 17% to 19%.



**Figure 10:** Heat production from CO + O recombination at two conditions: at 100 mbar data, only 2.2 W is lost within the measured region, and at 300 mbar just 48 W is lost via this channel.

#### 4.3.2 Estimated atomic O molar fractions and re-heating at increased pressure

With CO losses via R5 along the length of the tube deemed negligible, other estimates can be made using the CO flame band data. Given that the  $[CO][O]$  product and  $T$  are known, and the CO content in the gas stream is not expected to change significantly at  $z > 53$  mm, an estimate for  $[O]$  can be extracted. In Table 1, the CO molar fraction  $\chi_{CO,final}$  measured far downstream using mass spectrometry [21] is used to divide the molar fraction product  $\overline{\chi}_{CO} \cdot \overline{\chi}_{O,start} = [CO][O]/n_0^2$  and obtain an estimate of the atomic O molar fraction  $\overline{\chi}_{O,start,est}$  at  $z = 53$  mm in Figure 9. Clearly, atomic O molar fractions are at most  $\sim 1\%$ , with almost no atomic O present at 300 mbar and 12 slm. At 300 mbar atomic O recombination via



undoubtedly proceeds at a higher rate compared to 100 mbar. R10 lacks an activation energy and its rate is, therefore, not significantly enhanced with increasing  $T$ . The highest atomic O concentrations present also at 300 mbar, but at 6 slm, implies that additional production of atomic O occurs between plasma and  $z = 53$  mm. The likely contender for this process is



which possesses an equilibrium constant of  $k_8^+/k_8^- = 0.14 \cdot e^{\frac{2500}{T}}$  [26]. While the probability of R11 towards the production of O decreases with increasing  $T$ , the higher concentrations of O at 300 mbar, 6 slm likely result from a higher initial conversion of  $\text{CO}_2$  to CO at the height of the plasma: the rate of R11 towards the right-hand-side is enhanced due to higher  $[\text{CO}][\text{O}_2]$  compared to  $[\text{CO}_2][\text{O}]$ . This, in turn, leads to an increased rate for R10. In essence, an overproduction of CO at the height of the plasma is returned as a delayed re-heating of the gas stream downstream. This is why, in Figure 9, the temperatures are significantly higher at 300 mbar, 6 slm, compared to 300 mbar, 12 slm, despite the former having had a longer time-of-flight from the bottom of the plasma.

**Table 1:** Estimated radial mean atomic O concentrations  $\bar{X}_{\text{O},\text{start,est}}$  at  $z = 53$  mm for the conditions of Figure 9.  $X_{\text{CO},\text{final}}$  is based on mass spectrometry  $\sim 2$  m downstream of the plasma [21] and  $\bar{X}_{\text{CO}} \cdot \bar{X}_{\text{O},\text{start}}$  is derived from the radial mean of afterglow emission intensity  $I_\gamma$  at  $z = 53$  mm,  $\bar{X}_{\text{O},\text{start,est}}$  is obtained assuming  $X_{\text{CO},\text{final}} \approx X_{\text{CO},\text{start}}$ .

$p$ [mbar]	$P$ [W]	Flow [slm]	SEI [eV/molecule]	$X_{\text{CO},\text{final}}$ [-]	$\bar{X}_{\text{CO}} \cdot \bar{X}_{\text{O},\text{start}}$ [-]	$\bar{X}_{\text{O},\text{start,est}}$ [-]
100	860	6	2.0	0.20	$1.1 \cdot 10^{-3}$	$5.5 \cdot 10^{-3}$
100	860	12	1.0	0.11	$0.68 \cdot 10^{-3}$	$6.3 \cdot 10^{-3}$
300	1300	6	3.0	0.16	$0.21 \cdot 10^{-3}$	$13 \cdot 10^{-3}$
300	1300	12	1.5	0.13	$6.4 \cdot 10^{-7}$	$4.8 \cdot 10^{-6}$

### 4.3.3 Heat lost to the environment in the early afterglow

With gas compositions relatively stable at  $z \geq 53$  mm and assumed to consist mainly of  $\text{CO}_2$ , CO and  $\text{O}_2$ , and temperatures at the start of the measured afterglows known, the heat lost between plasma and  $z = 53$  mm can be estimated. Here, it is assumed that the mass flow profile along the width of the tube is flat, as calculated using Ansys Fluent in [21]. Combining the enthalpy for  $\text{CO}_2$ , CO and  $\text{O}_2$  as a function of temperature with the CO and  $\text{O}_2$  concentrations based on  $X_{\text{CO},\text{final}}$ , the power contained within the flow at  $z = 53$  mm is calculated. Table 2 lists the total power,  $P_{\text{total}}$ , the power contained in chemical enthalpy,  $P_{\text{chem}}$ , and the power contained in heat,  $P_{\text{heat}}$ . One additional parameter is estimated: the fraction of the heat generated in the plasma that was already released to the environment prior to  $z = 53$  mm. To obtain this fraction, it is assumed that at the height of the plasma 60% of the input power  $P$  goes towards heating the gas and 40% towards  $\text{CO}_2$  dissociation, calculated using the  $\text{CO}_2$  plasma reactor model in [21]. Comparing the numbers in Table 2, higher flow rates still contain more power at  $z = 53$  mm than lower flow rates. This is especially apparent for the 100 mbar, 12 slm condition, where very little of the initial 860 W has been lost to the environment. This is again reflected in the 27% fraction of heat lost, which for all other conditions is above 70%. Since this remarkable difference coincides with the 100 mbar, 12 slm condition having the highest energy efficiency of  $\eta = 35\%$ , this implies that removing heat from the system too fast may reduce the formation of CO. This conclusion is based on the fact that at this condition  $\bar{T}_{\text{start}} = 1260$  K is already below the level required to freeze in CO, while most of the heat in the gas is still to be removed from the system; thus, between plasma and  $z = 53$  mm a region of optimal composition and temperature must exist that maximizes CO and minimizes  $T$  (i.e. maximizing  $\eta$ ). The chemistry in this region could be elucidated further once our method for afterglow analysis is extended towards higher temperatures and variable gas compositions.

**Table 2:** Radial mean gas temperatures  $\bar{T}_{start}$  at  $z = 53$  mm, power contained within the flow at  $z = 53$  mm,  $P_{total}$ , its subdivision into power contained in chemical enthalpy,  $P_{chem}$ , and heat,  $P_{heat}$ , and the fraction of heat already cooled away at  $z < 53$  mm. The latter assumes 40% of the input power  $P$  initially goes towards chemistry and 60% towards heating the gas [21].

$p$ [mbar]	$P$ [W]	Flow [slm]	SEI [eV/molecule]	$\bar{T}_{start}$ [K]	$P_{total}$ [W]	$P_{chem}$ [W]	$P_{heat}$ [W]	Fraction of heat lost at $z < 53$ mm [%]
100	860	6	2.0	1120	445	274	171	0.71
100	860	12	1.0	1260	711	299	412	0.27
300	1300	6	3.0	1507	480	211	269	0.75
300	1300	12	1.5	993	627	347	280	0.71

## 5. Summary & Conclusions

We have investigated CO flame band emission ( $\text{CO} + \text{O} \rightarrow \text{CO}_2 + h\nu$ ) in pure  $\text{CO}_2$  microwave plasma by obtaining absolute emission spectra at various locations in the plasma afterglow while simultaneously measuring gas temperatures using rotational Raman scattering. An empirical model for simulating these spectra was constructed by fitting the Arrhenius equation to the absolute emission as a function of gas temperature at various wavelengths between 260 – 700 nm. With the spectrum shape depending strongly on gas temperature, a method for easily obtaining gas temperatures surrounding the plasma is obtained.

Comparison of our results to literature for CO flame band emission obtained in  $\text{CO}/\text{O}_2$  flames and shock tubes reveal a much stronger UV component emerging in our spectra at temperatures  $> 1500$  K. This UV component is consistent with  $\text{O}_2$  Schumann-Runge emission and likely results from the collisional exchange of internal energy between  $\text{CO}_2(^1\text{B})$  and  $\text{O}_2$ . Thus, with the UV component dependent on the  $\text{O}_2$  fraction in the gas, our empirical model for afterglow emission cannot be directly applied at all conditions. In a follow-up study, the composition of the gas will be measured in addition to the absolute emission spectra by using a new rotational Raman scattering technique [19], allowing for reliable extension of the afterglow emission model to higher temperatures.

To demonstrate our method, afterglow emission starting at  $\sim 3$  cm downstream of the  $\text{CO}_2$  microwave plasma is analyzed, where temperatures are sufficiently low to apply the current empirical model. The resulting temperature maps showed large variations in the distribution of gas temperature with pressure and flow rate. The amount of heat generated through  $\text{CO} + \text{O} + \text{M} \rightarrow \text{CO}_2 + \text{M}$  was calculated as 2.2 W at 860 W, 100 mbar, 6 slm and 48 W at 1300 W, 300 mbar, 6 slm. Since this represents a negligible loss of CO, measurements of CO densities further downstream could be used to evaluate compositions at  $\sim 3$  cm from the plasma. This analysis revealed  $< 1\%$  atomic O for all conditions, with the highest pressure and lowest flow rates (300 mbar, 6 slm) maintaining the most atomic O towards the downstream region. We argue that this maximizing of atomic O results from an overproduction of CO at the height of the plasma, thus pushing the balance of the  $\text{CO} + \text{O}_2 \leftrightarrow \text{CO}_2 + \text{O}$  reaction towards the right-hand-side in the early afterglow. The additional atomic O thus produced leads to additional heating downstream of the plasma after recombination to molecular  $\text{O}_2$ . This same process is seen to be avoided when doubling the flow from 6 to 12 slm, since the CO produced in the plasma becomes significantly diluted by additional  $\text{CO}_2$  and temperatures remain significantly lower beyond  $\sim 3$  cm downstream. The highest energy efficiency for CO production is shown to coincide with an operating

condition (860 W, 100 mbar, 12 slm) where very little heat has been lost to the environment prior to  $\sim 3$  cm downstream. This implies that removing heat from the system as fast as possible post-plasma is not necessarily beneficial, but that a region can be formed in which an optimal composition and temperature exists that maximizes CO and minimizes  $T$  without significant cooling to the environment. At 860 W, 100 mbar, 12 slm, this region ends at a temperature  $T \approx 1260$  K within 3 cm of the plasma; already below the level required to effectively freeze in CO and thus precluding the need for a sophisticated downstream cooling method.

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## Supplementary information

### Flame Bands: CO + O chemiluminescence as a measure of gas temperature

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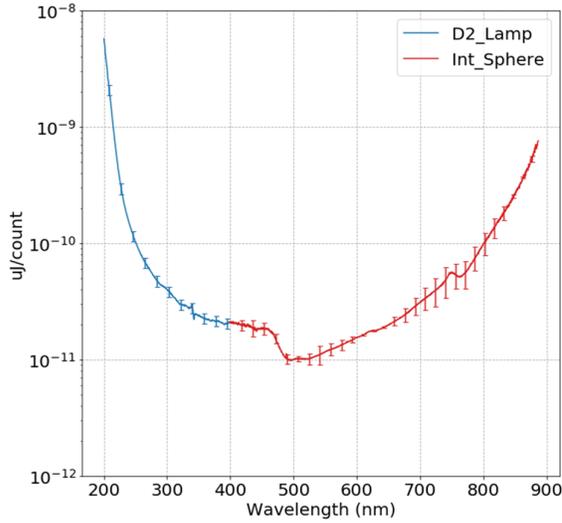
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#### S.1: Calibration curve of the optical system + half quartz tube



**Figure S.1.1:** Calibration curve for the optical system in  $\mu\text{J}/\text{count}$  obtained using a halogen lamp with integrating sphere for visible wavelengths (red) and a deuterium lamp in the UV range (blue). A lower value on the y-axis implies a higher sensitivity.

#### S.2: Derivations of Eq. (2) and Eq. (8) in the main text

Using the reaction chain R1 – R4, the recombination rate coefficient  $k_{rec}$  for the overall reaction R5 can be found from the reaction equations for  $\text{CO}_2(1^1\text{B})$  and  $\text{CO}_2(1^3\text{B})$  and assuming steady-state:

$$\frac{\partial[\text{CO}_2(^3\text{B})]}{\partial t} = k_1^+[\text{CO}][\text{O}][\text{M}] - (k_1^-[\text{M}] + k_2^+[\text{M}])(\text{CO}_2(^3\text{B})) = 0 \quad \text{and} \quad (\text{S.1})$$

$$\frac{\partial[\text{CO}_2(^1\text{B})]}{\partial t} = k_2^+[\text{CO}_2(^3\text{B})][\text{M}] - (k_2^-[\text{M}] + k_3^+[\text{M}] + k_4^+)[\text{CO}_2(^1\text{B})] = 0, \quad (\text{S.2})$$

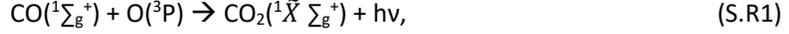
where the simplified notation for the two electronically excited states is used.

Realizing that the change in ground state  $\text{CO}_2$  is equal to the rate of reaction R5 and substituting the solutions for  $[\text{CO}_2(^1\text{B})]$  and  $[\text{CO}_2(^3\text{B})]$  from (S.1) and (S.2) we get:

$$\frac{\partial[\text{CO}_2]}{\partial t} = k_{rec}[\text{CO}][\text{O}][\text{M}] = (k_3^+[\text{M}] + k_4^+)[\text{CO}_2(^1\text{B})]$$

$$= \frac{k_1^+ k_2^+ [M] (k_3^+ [M] + k_4^+)}{(k_1^- [M] + k_2^+ [M]) (k_2^- [M] + k_3^+ [M] + k_4^+)} [\text{CO}][\text{O}][\text{M}]. \quad (\text{S.3})$$

For the rate coefficient  $k_\gamma$  for the overall reaction leading to photon emission



it suffices to substitute the solution for  $[\text{CO}_2(^3\text{B})]$  from (S.2) into (S.1) and obtain a solution for  $[\text{CO}_2(^1\text{B})]$ . Mutiplying this result by the rate coefficient  $k_4^+$  then provides the rate of photon emission:

$$\begin{aligned} I_\gamma &= k_\gamma [\text{CO}][\text{O}] = k_4^+ [\text{CO}_2(^1\text{B})] \\ &= \frac{k_1^+ k_2^+ [M] k_4^+ [M]}{(k_1^- [M] + k_2^+ [M]) (k_2^- [M] + k_3^+ [M] + k_4^+)} [\text{CO}][\text{O}]. \end{aligned} \quad (\text{S.4})$$

Assuming spontaneous emission via R4 is slower than the (quenching) reaction steps of R2 and R4, the results of Eqs. (S.3) and (S.4) can be further simplified to:

$$k_{rec} = \frac{k_1^+ k_2^+ k_3^+}{(k_1^- + k_2^+) (k_2^- + k_3^+)} \quad \text{and} \quad (\text{S.5})$$

$$k_\gamma = \frac{k_1^+ k_2^+ k_4^+}{(k_1^- + k_2^+) (k_2^- + k_3^+)}, \quad (\text{S.6})$$

so that

$$\frac{k_{rec}}{k_\gamma} = \frac{k_3^+}{k_4^+}. \quad (\text{S.7})$$

For  $\text{O}_2$  Schumann-Runge emission, the rate equation for  $\text{O}_2(^3\text{B})$  via R6 – R8 is:

$$\frac{\partial[\text{O}_2(^3\text{B})]}{\partial t} = k_6^+ [\text{CO}_2(^1\text{B})][\text{O}_2] - (k_7^+ [\text{M}] + k_8^+) [\text{O}_2(^3\text{B})] = 0, \quad (\text{S.8})$$

which is easily solved to obtain the rate of photon emission from excited  $\text{O}_2$ :

$$I_\gamma^{O_2} = \frac{k_6^+ k_8^+ [\text{CO}_2(^1\text{B})][\text{O}_2]}{k_7^+ [\text{M}] + k_8^+} \approx \frac{k_6^+ k_8^+}{k_7^+} \mathcal{X}_{O_2} [\text{CO}_2(^1\text{B})] \approx \frac{k_6^+ k_8^+}{k_4^+ k_7^+} \mathcal{X}_{O_2} \cdot k_\gamma [\text{CO}][\text{O}]. \quad (\text{S.9})$$

As (S.9) shows, the rate of UV photon emission will be proportional to photon emission from  $\text{CO} + \text{O}$  recombination, scaled by the  $\text{O}_2$  fraction in the gas.

Alternatively, if  $\text{O}_2(^3\text{B})$  results from quenching of  $[\text{CO}_2(^3\text{B})]$  by  $\text{O}_2$  via



we get:

$$\frac{\partial[\text{O}_2(^3\text{B})]}{\partial t} = k_{A,R3}^+ [\text{CO}_2(^3\text{B})][\text{O}_2] - (k_7^+ [\text{M}] + k_8^+) [\text{O}_2(^3\text{B})] = 0, \quad (\text{S.10})$$

which can be solved by substituting the result of (S.1) to obtain an alternative rate of photon emission  $I_{\gamma}^{O_2}$ :

$$I_{\gamma}^{O_2} = \frac{k_{S.R2}^+ k_8^+ [CO_2(^3B)][O_2]}{k_7^+ [M] + k_8^+} = \frac{k_1^+ k_{S.R2}^+ k_8^+ [O_2]}{(k_1^- + k_2^+) (k_7^+ [M] + k_8^+)} [CO][O] \approx \frac{k_1^+ k_{S.R2}^+ k_8^+}{(k_1^- + k_2^+) k_7^+} \chi_{O_2} [CO][O], \quad (S.11)$$

which has the same general features as (S.9).

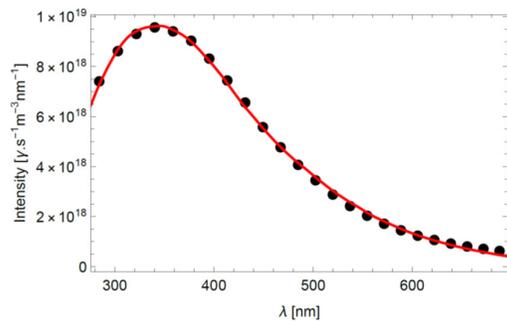
### S.3 Values of Arrhenius model

**Table S.1:** Tabulated values from Arrhenius fits displayed in Figure 6 of the main text.

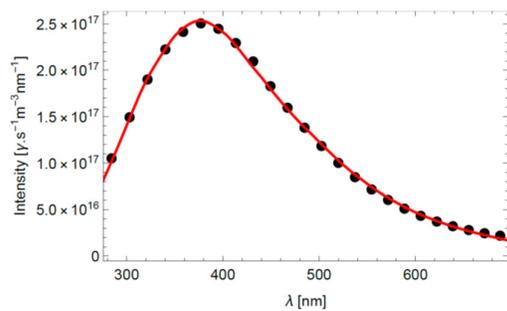
$\lambda$ [nm]	$k_0^\lambda$ [ $10^{-27} \gamma \cdot m^3 s^{-1} nm^{-1}$ ]	$\Delta k_0^\lambda$ [ $10^{-27} \gamma \cdot m^3 s^{-1} nm^{-1}$ ]	$E_a^\lambda$ [K]	$\Delta E_a^\lambda$ [K]
246.5	16.415	3.92132	5766	120.9
255.9	16.0996	3.41351	5399	107.8
265.4	15.2869	2.71347	5007	91.11
274.8	13.988	2.07875	4591	76.89
284.3	12.4721	1.51714	4188	63.48
293.6	10.8797	1.05643	3781	50.99
303	9.44795	0.68466	3411	38.48
312.3	8.12461	0.43003	3065	28.31
321.7	7.01463	0.25935	2752	19.88
331	6.15028	0.15927	2487	14.05
340.2	5.4499	0.08542	2253	8.493
349.5	4.83653	0.09163	2051	10.38
358.7	4.35227	0.09219	1884	11.64
367.8	3.92159	0.09918	1738	13.99
377	3.53459	0.10552	1613	16.63
386.1	3.20335	0.11108	1510	19.35
395.2	2.92706	0.12281	1430	23.37
404.3	2.63952	0.11351	1345	24.25
413.4	2.39025	0.11172	1277	26.55
422.4	2.1758	0.10662	1226	27.75
431.4	2.00511	0.10141	1185	28.84
440.4	1.84448	0.09381	1156	28.87
449.3	1.69486	0.08878	1124	29.88
458.2	1.56894	0.08297	1102	30.18
467.1	1.45586	0.07703	1086	30.28
476	1.3652	0.06988	1085	29.37
484.8	1.28711	0.06198	1088	27.41
493.6	1.19877	0.05717	1088	26.98
502.4	1.10672	0.05433	1071	27.9
511.2	1.03169	0.05257	1072	28.86
519.9	0.96387	0.04508	1081	26.56
528.6	0.90746	0.04118	1094	25.79

537.2	0.85035	0.03872	1099	25.95
545.9	0.7827	0.03768	1088	27.55
554.5	0.72513	0.03663	1085	28.94
563	0.68523	0.03738	1103	31.18
571.6	0.6414	0.03229	1108	28.92
580.1	0.59852	0.03086	1113	29.68
588.6	0.5561	0.02914	1107	30.29
597	0.52241	0.02909	1114	32.21
605.5	0.49115	0.02493	1119	29.52
613.9	0.46575	0.02526	1139	31.51
622.2	0.43867	0.02098	1141	27.83
630.6	0.4147	0.02127	1153	29.96
638.9	0.39047	0.01891	1156	28.37
647.1	0.36891	0.01904	1162	30.28
655.4	0.35011	0.01722	1170	28.92
663.6	0.33244	0.01506	1179	26.72
671.8	0.31695	0.01418	1198	26.47
679.9	0.30222	0.01292	1216	25.29
688	0.28921	0.01129	1240	23.11
696.1	0.27912	0.01115	1272	23.66

#### S.4 Example Arrhenius model fits



**Figure S.2:** Spectrum fit for 300 mbar, 6 slm at  $r = -4$  mm and  $z = 53$  mm. Fitted temperature is  $(1869.65 \pm 45.81)$  K.



**Figure S.2:** Spectrum fit for 100 mbar, 12 slm at  $r = -2$  mm and  $z = 53$  mm. Fitted temperature is  $(1260.02 \pm 22.69)$  K.